PROBABILITY AND MATHEMATICAL STATISTICS Vol. 19, Fasc. 1 (1999), pp. 97–104

DECOMPOSITION OF CONVOLUTION SEMIGROUPS ON GROUPS AND THE 0-1 LAW

H. Byczkowska T. Byczkowski

Abstract: Let $(X(t))_{t>0}$ be a stochastically continuous symmetric Lévy process with values in a complete separable group G. We denote by $(\mu_t)_{t>0}$ the semigroup of one-dimensional distributions of X(t). Suppose that H is a Borel subgroup of Gsuch that $\mu_t(H) > 0$ for all t > 0. We obtain a decomposition of the generator of the process X(t) into a bounded part concentrated on H^c and the generator of a semigroup concentrated on H. This yields the 0 - 1 law for such processes. We also examine the differentiation of transition probability of the induced Markov process $\pi(X(t))$ on the homogeneous space G/H.

2000 AMS Mathematics Subject Classification: Primary: -; Secondary: -; Key words and phrases: -

THE FULL TEXT IS AVAILABLE HERE