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OCCUPATION TIME FLUCTUATIONS OF POISSON AND EQUILIBRIUM BRANCHING SYSTEMS IN CRITICAL AND LARGE DIMENSIONS

Piotr MiŁoś

Abstract: Limit theorems are presented for the rescaled occupation time fluctuation process of a critical finite variance branching particle system in \mathbb{R}^d with symmetric α -stable motion starting off from either a standard Poisson random field or the equilibrium distribution for critical $d=2\alpha$ and large $d>2\alpha$ dimensions. The limit processes are generalised Wiener processes. The obtained convergence is in space-time and finite-dimensional distributions sense. Under the additional assumption on the branching law we obtain functional convergence.

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